

Figure 1: Drop in liquids pressure at distance L, as it flows through a pipe of diameter D.

# Hydraulic pressure loss coefficient<sup>1</sup>

key words: Pressure loss, turbulent and laminar friction coefficient, Blasius' equation, Nikuradse or Moody diagram.

goals: The objective of this exercise is to measure pressure loss coefficient for an incompressible, turbulent and laminar flow through a pipeline.

## 1 Introduction

Any real life engineering phenomena is accompanied by energy dissipation. It is no different with a real fluid in motion. In case of a liquid flowing through a straight pipe energy losses are an effect of shear stresses ( $\tau$ ) acting against the flow. Those energy losses manifest itself by drop in **hydraulic head**<sup>2</sup> at consecutive cross-sections of the flow, and are referred to as **head losses**<sup>3</sup>. This is shown in Fig.1.

Pressure losses  $\Delta p_{loss}$  resulting from liquid's flow through a pipe of diameter D and length L are proportional to liquids dynamic pressure. And are defined by the so called **Darcy-Weisbach equation** 

$$\Delta p_{loss} = \lambda \frac{L}{D} \frac{\rho V^2}{2} \tag{1}$$

The proportionality coefficient  $\lambda$  is the so called **Darcy friction factor**.

<sup>&</sup>lt;sup>1</sup>In English nomenclature **Darcy friction factor**.

 $<sup>^2\</sup>mathrm{Pressure}$  expressed as **hight** of a static column of fluid. Expressed in meters, millimeters ...

<sup>&</sup>lt;sup>3</sup>Also referred to as resistance head or friction head





Friction coefficient  $\lambda$  varies strongly with the Reynolds number<sup>4</sup>. For laminar flows (Re < 2300) it might be calculated analytically from Hagen-Poiseuille equation to be:

$$\lambda = \frac{64}{Re} \tag{2}$$

However for turbulent flows empirical formulas are used. A good approximation is given by the Blasius<sup>5</sup> formula (for flows where  $Re < 8 * 10^4$ ):

$$\lambda = \frac{0.316}{\sqrt[4]{Re}} \tag{3}$$

Equation 1 and 2 are valid only in case of **smooth** and **circular** pipes. In case of rough surfaces values of the friction factor are found by experiment. Such experiment were performed by Johann Nikuradse<sup>6</sup>. Figure 1 shows the so called Nikuradse diagram<sup>7</sup> relating friction factor  $\lambda$ , Reynolds number and relative roughness of the pipe.

## 2 Measurements and calculations

Using the experimental setups for laminar and turbulent flows investigate pressure losses. Perform appropriate measurements and calculations.

#### 2.1 Pressure loss coefficient for turbulent flow

- 1. Get acquainted with the experimental setup, check how manometers are connected and what is being measured.
- 2. Copy all the necessary dimensions of the investigated installation to your report.
- 3. Start the flow through the installation, manipulate the flow rate with a valve.
- 4. Using a stopwatch measure a time t necessary to fill the reference tank of volume V.
- 5. Note the pressure losses.

 $<sup>{}^{4}</sup>Re = \frac{V * D}{\nu}$ , Pipe diameter D is used as characteristic length.

<sup>&</sup>lt;sup>5</sup>Paul Richard Heinrich Blasius (1883-1970) was a German fluid dynamics engineer. <sup>6</sup>Johann Nikuradse (November 20, 1894 July 18, 1979) Georgia-born German engineer and physicist.Lived mostly in Gttingen.

<sup>&</sup>lt;sup>7</sup>In English nomenclature **Moody chart**.

- 6. Repeat the measurements at different flow rates. Ask the tutor for the number of test you should perform.
- 7. Stop the flow through the installation when finished.
- 8. Note water temperature.
- 9. For each of the measurements calculate: pressure loss, flow velocity, Reynolds number and friction factor  $\lambda$ .
- 10. Plot the results on a  $\lambda(Re)$  plot, and compare with Blasius formula 3.
- 11. Comment on the results.

### 2.2 Pressure loss coefficient for laminar flow

- 1. Get acquainted with the experimental setup, check how manometers are connected and what is being measured.
- 2. Copy all the necessary dimensions to your report.
- 3. Start the flow, manipulate the flow rate by changing hight H of the water source.
- 4. Using a stopwatch measure a time t necessary to fill graduated cylinder used for reference.
- 5. Measure the pressure drop.
- 6. Repeat the measurements at different flow rates. Ask the tutor for the number of test you should perform.
- 7. Note water temperature.
- 8. For each of the measurements calculate: pressure loss, flow velocity, Reynolds number and friction factor  $\lambda$ .
- 9. Plot the results on a  $\lambda(Re)$  plot, and compare with formula 2.
- 10. Comment on the results.

Dear student,

should you have any remarks, observations or comments concerning this instruction. Please do not hesitate to make them.